

1-5 Practice

Solving Inequalities

Form K

Write the inequality that represents the sentence.

1. Five less than a number is at least -28.

$$x - 5 \geq -28$$

2. The product of a number and four is at most -10.

$$4x \leq -10$$

3. Six more than a quotient of a number and three is greater than 14.

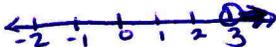
$$\frac{x}{3} + 6 > 14$$

Solve each inequality. Graph the solution.

4. $5a - 10 > 5$

To start, add 10 to each side.

$$a > 3$$



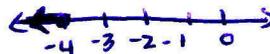
6. $-2(n + 2) + 6 \leq 16$

$$n \geq -7$$



5. $25 - 2y \geq 33$

$$y \leq -4$$



7. $2(7a + 1) > 2a - 10$

$$a > -1$$



Solve the following problem by writing an inequality.

8. The width of a rectangle is 4 cm less than the length. The perimeter is at most 48 cm. What are the restrictions on the dimensions of the rectangle?

To start, record what you know.

width: length - 4

Describe what you need to find.

perimeter: at most 48 cm

restrictions on the width and

length of the rectangle

The length of the rectangle is at most 14 cm and the width is at most 10 cm

Is the inequality *always*, *sometimes*, or *never* true?

9. $5(x - 2) \geq 2x + 1$

Sometimes

10. $2x + 8 \leq 2(x + 1)$

never

11. $6x + 1 < 3(2x - 4)$

never

12. $2(3x + 3) > 2(3x + 1)$

always

1-5 Practice (continued)

Solving Inequalities

Form K

Solve each compound inequality. Graph the solution.

13. $2x > -4$ and $4x < 12$

To start, simplify each inequality. $x > -2$ and $x < 3$

Remember, "and" means that a solution makes BOTH inequalities true.

$x > -2$ and $x < 3$

$-2 < x < 3$



14. $3x \geq -12$ and $5x \leq 5$

$x \geq -4$ and $x \leq 1$

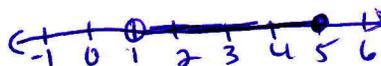
$-4 \leq x \leq 1$



15. $6x > 6$ and $9x \leq 45$

$x > 1$ and $x \leq 5$

$1 < x \leq 5$



Solve each compound inequality. Graph the solution.

16. $3x < -9$ or $8x > -8$

To start, simplify each inequality. $x < -3$ or $x > -1$

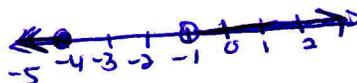
Remember, "or" means that a solution makes EITHER inequality true.

$x < -3$ or $x > -1$



17. $7x \leq -28$ or $2x > -2$

$x \leq -4$ or $x > -1$



18. $3x > 3$ or $5x < 2x - 3$

$x > 1$ or $x < -1$



Write an inequality to represent each sentence.

19. The average of Shondra's test scores in Physics is between 88 and 93.

Let x = Shondra's test score average

$88 < x < 93$

20. The Morgans are buying a new house. They want to buy either a house more the 75 years old or a house less than 10 years old.

Let x = age of house

$x < 10$ or $x > 75$

$$\begin{array}{r|l}
 4. \quad 5a - 10 > 5 \\
 +10 \quad +10 \\
 \hline
 5a > 15 \\
 \frac{5a}{5} > \frac{15}{5} \\
 a > 3
 \end{array}$$

$$\begin{array}{r|l}
 5. \quad 25 - 2y \geq 33 \\
 -25 \quad -25 \\
 \hline
 -2y \geq 8 \\
 \frac{-2y}{-2} \geq \frac{8}{-2} \\
 y \leq -4
 \end{array}$$

$$\begin{array}{r|l}
 6. \quad -2(n+2) + 6 \leq 16 \\
 -2n - 4 + 6 \leq 16 \\
 -2n + 2 \leq 16 \\
 -2 \quad -2 \\
 \hline
 -2n \leq 14 \\
 \frac{-2n}{-2} \leq \frac{14}{-2} \\
 n \geq -7
 \end{array}$$

$$\begin{array}{r|l}
 7. \quad 2(7a+1) > 2a-10 \\
 14a+2 > 2a-10 \\
 -2a \quad -2a \\
 \hline
 12a+2 > -10 \\
 -2 \quad -2 \\
 \hline
 12a > -12 \\
 \frac{12a}{12} > \frac{-12}{12} \\
 a > -1
 \end{array}$$

8. Let x = length of rectangle
 then $x-4$ = width of rectangle

$$\begin{array}{r|l}
 2(x) + 2(x-4) \leq 48 \\
 2x + 2x - 8 \leq 48 \\
 4x - 8 \leq 48 \\
 +8 \quad +8 \\
 \hline
 4x \leq 56 \\
 \frac{4x}{4} \leq \frac{56}{4} \\
 x \leq 14
 \end{array}$$

$$\begin{array}{r|l}
 9. \quad 5(x-2) & \geq 2x+1 \\
 5x-10 & \geq 2x+1 \\
 -2x & -2x \\
 \hline
 3x-10 & \geq 1 \\
 +10 & +10 \\
 \hline
 3x & \geq 11 \\
 \frac{3x}{3} & \geq \frac{11}{3} \\
 x & \geq \frac{11}{3}
 \end{array}$$

$$\begin{array}{r|l}
 10. \quad 2x+8 & \leq 2(x+1) \\
 2x+8 & \leq 2x+2 \\
 -2x & -2x \\
 \hline
 8 & \leq 2
 \end{array}$$

$$\begin{array}{r|l}
 11. \quad 6x+1 & < 3(2x-4) \\
 6x+1 & 6x-12 \\
 -6x & -6x \\
 \hline
 1 & < -12
 \end{array}$$

$$\begin{array}{r|l}
 12. \quad 2(3x+3) & > 2(3x+1) \\
 6x+6 & > 6x+2 \\
 -6x & -6x \\
 \hline
 6 & > 2
 \end{array}$$

$$\begin{array}{r|l}
 13. \quad \frac{2x}{2} > \frac{-4}{2} \text{ and } \frac{4x}{4} < \frac{12}{4} \\
 x > -2 & x < 3
 \end{array}$$

$$\begin{array}{r|l}
 14. \quad \frac{3x}{3} \geq \frac{-12}{3} \text{ and } \frac{5x}{5} \leq \frac{5}{5} \\
 x \geq -4 & x \leq 1
 \end{array}$$

$$\begin{array}{r|l}
 15. \quad \frac{6x}{6} > \frac{6}{6} \text{ and } \frac{9x}{9} \leq \frac{45}{9} \\
 x > 1 & x \leq 5
 \end{array}$$

$$\begin{array}{r|l}
 16. \quad \frac{3x}{3} < \frac{9}{3} \text{ or } \frac{8x}{8} > \frac{-8}{8} \\
 x < 3 & x > -1
 \end{array}$$

$$\begin{array}{r|l}
 17. \quad \frac{7x}{7} \leq \frac{-28}{7} \text{ or } \frac{2x}{2} > \frac{-2}{2} \\
 x \leq -4 & x > -1
 \end{array}$$

$$\begin{array}{r|l}
 18. \quad \frac{3x}{3} > \frac{3}{3} \text{ or } \frac{5x}{5} < \frac{2x-3}{5} \\
 x > 1 & \frac{-2x}{5} < \frac{-2x-3}{5} \\
 & \frac{3x}{3} < \frac{-3}{3} \\
 & x < -1
 \end{array}$$